

Λύσεις Β λυκείου 17-04-2022

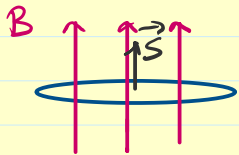
ΘΕΜΑ Α

A1 γ A2 γ A3 δ A4 α

A5 α) ς β) ς γ) ς δ) ς ε) ς

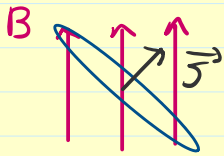
ΘΕΜΑ Β

B1 Λύση απάντηση: β



$$\Phi_{\text{αρχ}} = B \cdot S \cdot \cos 0^\circ = B \cdot S$$

→ Στρέφεται κατά 60°

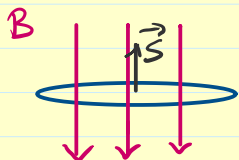


$$\Phi_{\text{τελ}} = B \cdot S \cdot \cos 60^\circ = \frac{B \cdot S}{2}$$

$$|\Delta \Phi| = |\Phi_{\text{τελ}} - \Phi_{\text{αρχ}}| = \left| \frac{B \cdot S}{2} - B \cdot S \right| = \frac{B \cdot S}{2}$$

$$\mathcal{E}_{\text{ηλ}} = N_1 \cdot \frac{|\Delta \Phi|}{\Delta t} \Rightarrow \mathcal{E}_{\text{ηλ}} = N_1 \cdot \frac{B \cdot S}{2 \Delta t} \quad (1)$$

→ Αντιστρέφεται η μαγνητική επαγωγή



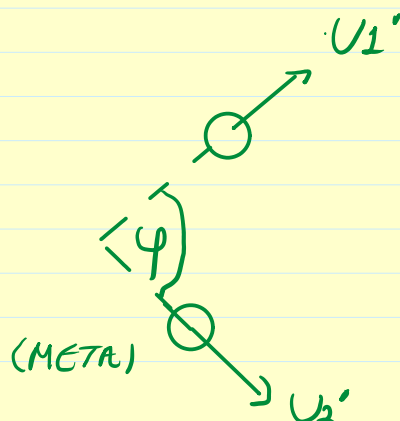
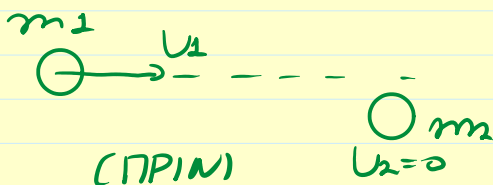
$$\Phi_{\text{τελ}} = B \cdot S \cdot \cos 180^\circ = -B \cdot S$$

$$|\Delta \Phi| = |\Phi_{\text{τελ}} - \Phi_{\text{αρχ}}| = |-B \cdot S - B \cdot S| = 2 B \cdot S$$

$$\mathcal{E}_{\text{ηλ}} = N_2 \cdot \frac{|\Delta \Phi|}{\Delta t} \Rightarrow \mathcal{E}_{\text{ηλ}} = N_2 \cdot \frac{2 B \cdot S}{\Delta t} \quad (2)$$

$$(1) = (2) \Rightarrow N_1 \cdot \frac{B \cdot S}{2 \Delta t} = N_2 \cdot \frac{2 B \cdot S}{\Delta t} \Rightarrow N_2 = \frac{N_1}{4}$$

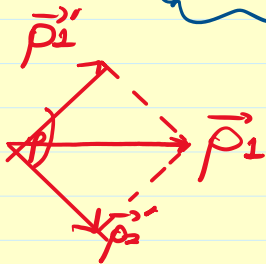
B2 Λύση απάντηση: γ



→ Σχέση K-p

$$K = \frac{1}{2} m v^2 = \frac{1}{2} \cdot \frac{m \cdot m \cdot v^2}{m} = \frac{(m \cdot v)^2}{2m} = \frac{p^2}{2m}$$

→ A.D.O. : $\vec{p}_1 + \vec{p}_2^0 = \vec{p}_1' + \vec{p}_2'$



$$p_1^2 = p_1'^2 + p_2'^2 + 2 \cdot p_1' \cdot p_2' \cdot \cos \varphi \quad (1)$$

→ A.D.K.E.

$$K_1 + K_2^0 = K_1' + K_2' \Rightarrow \frac{p_1^2}{2m_1} = \frac{p_1'^2}{2m_1} + \frac{p_2'^2}{2m_2}$$

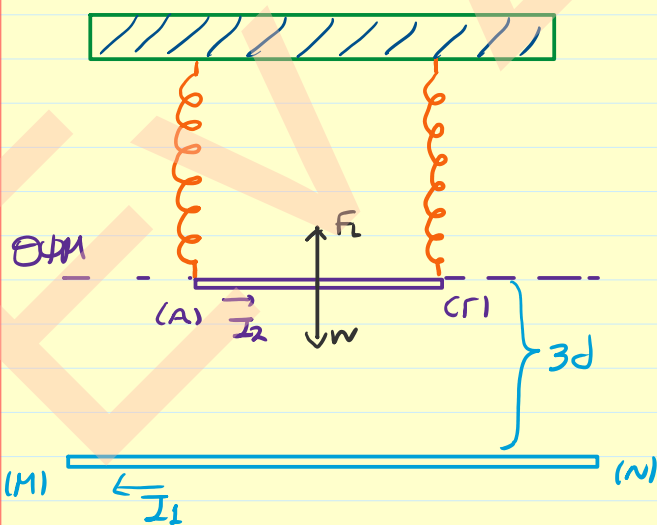
$$\Rightarrow p_1^2 = p_1'^2 + p_2'^2 \quad (2)$$

$$(1) \stackrel{(2)}{\Rightarrow} p_1'^2 + p_2'^2 = p_1'^2 + p_2'^2 + 2 \cdot p_1' \cdot p_2' \cdot \cos \varphi$$

$$\Rightarrow 2 \cdot p_1' \cdot p_2' \cdot \cos \varphi = 0 \quad \underbrace{2 p_1' \cdot p_2' \neq 0}_{\text{}} \Rightarrow \cos \varphi = 0$$

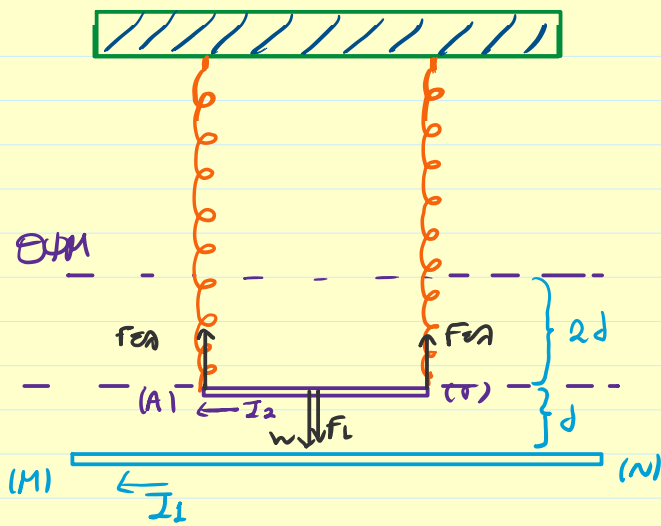
→ $\varphi = 90^\circ$

B3 Πύση απώρευση: α



$$\sum F = 0 \Rightarrow k_{\mu} \frac{2 I_1 \cdot I_2 \cdot l}{3d} = w$$

$$\Rightarrow k_{\mu} \frac{2 I_1 \cdot I_2 \cdot l}{d} = 3 \cdot w \quad (1)$$



$$2F=0 \Rightarrow f_l + w = F_{\text{I1}} + F_{\text{I2}}$$

$$\Rightarrow K_p \cdot \frac{2I_1 \cdot I_2 \cdot l}{d} + w = 2 \cdot F_{\text{I1}}$$

$$(1) \Rightarrow 3w + w = 2 \cdot k \cdot 2d$$

$$\Rightarrow 4w = 4k \cdot d$$

$$\Rightarrow \boxed{k = \frac{w}{d}}$$

ΘΕΜΑ Γ

Γ1 $U_p = i$, $t = 5s$

$$\omega = \alpha_{\text{γων1}} \cdot t = 4 \cdot 5 \Rightarrow \omega = 20 \text{ rad/s} \quad \rightarrow U_p = \omega \cdot R \Rightarrow \boxed{U_p = 10 \text{ m/s}}$$

Γ2 $\alpha_{\text{γων2}} = i$, $t_{\text{stop}} = ?$

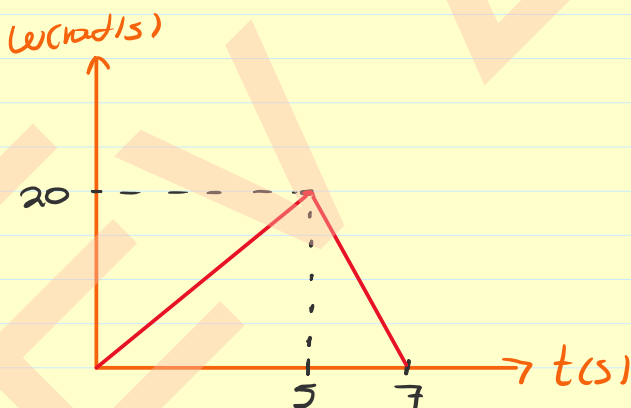
$$N_2 = \frac{\Delta\theta_2}{2\pi} = \frac{10}{\pi} \Rightarrow \Delta\theta_2 = 20 \text{ rad}$$

$$\Delta\theta_2 = \frac{\omega_0^2 - \omega^2}{2\alpha_{\text{γων2}}} \Rightarrow 20 = \frac{20^2}{2\alpha_{\text{γων2}}} \Rightarrow \boxed{\alpha_{\text{γων2}} = 10 \text{ rad/s}^2}$$

$$\omega = \omega_0 - \alpha_{\text{γων2}} \cdot \Delta t \Rightarrow 0 = 20 - 10 \cdot \Delta t \Rightarrow \Delta t = 2s$$

$$\Delta t = t_{\text{stop}} - 5 \Rightarrow \boxed{t_{\text{stop}} = 7s}$$

Γ3 $\omega - t$, $N = i$



$$\rightarrow 0-5s: \Delta\theta_1 = \frac{1}{2} \cdot \alpha_{\text{γων1}} \cdot t^2$$

$$\Rightarrow \Delta\theta_1 = \frac{1}{2} \cdot 4 \cdot 5^2 = 50 \text{ rad}$$

$$N_1 = \frac{\Delta\theta_1}{2\pi} = \frac{50}{2\pi} \Rightarrow N_1 = \frac{25}{\pi} \text{ σφρ.}$$

$$\rightarrow 5-7s: N_2 = \frac{10}{\pi} \text{ σφρ.}$$

$$\boxed{N_{\text{ολ}} = N_1 + N_2 = \frac{35}{\pi} \text{ σφρ.}}$$

Γ4 $S = ?$

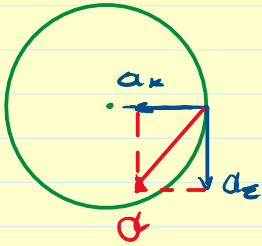
Από 3-4s:

$$\Delta\theta = \frac{1}{2} \alpha \omega^2 \cdot t^2 \quad \begin{cases} t=3s, & \Delta\theta_3 = \frac{1}{2} \cdot 4 \cdot 3^2 = 18 \text{ rad} \\ t=4s, & \Delta\theta_4 = \frac{1}{2} \cdot 4 \cdot 4^2 = 32 \text{ rad} \end{cases}$$

$$\Delta\theta = \Delta\theta_4 - \Delta\theta_3 = 14 \text{ rad}$$

$$S = R \cdot \Delta\theta = 0,5 \cdot 14 \Rightarrow \boxed{S = 7 \text{ m}}$$

$$\boxed{\Gamma 5} \quad t = 0,5 \text{ s}, \quad \alpha = ?$$



$$\omega = \alpha \omega^2 \cdot t = 4 \cdot 0,5 = 2 \text{ rad/s}$$

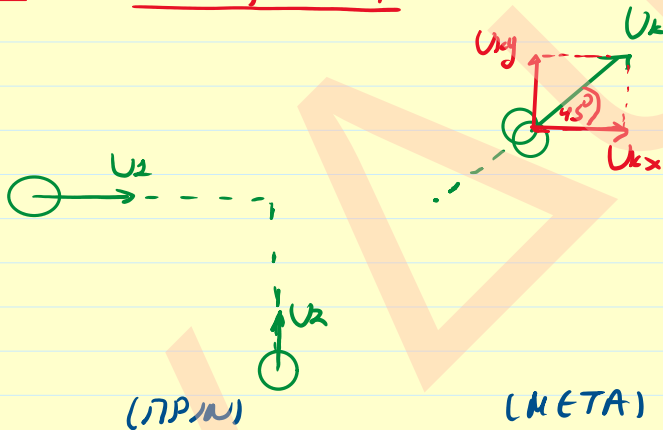
$$a_t = \omega^2 \cdot R = 2^2 \cdot 0,5 \Rightarrow a_t = 2 \text{ m/s}^2$$

$$a_c = \alpha \omega^2 \cdot R = 4 \cdot 0,5 \Rightarrow a_c = 2 \text{ m/s}^2$$

$$a = \sqrt{a_t^2 + a_c^2} = \sqrt{2^2 + 2^2} \Rightarrow \boxed{a = 2 \cdot \sqrt{2} \text{ m/s}^2}$$

ΘΕΜΑ Δ

$$\boxed{\Delta 1} \quad \alpha) \quad U_{K1} = ? , \quad U_2 = ?$$



$$U_{Kx} = U_K \cdot \sin 45^\circ = U_K \cdot \frac{\sqrt{2}}{2}$$

$$U_{Ky} = U_K \cdot \cos 45^\circ = U_K \cdot \frac{\sqrt{2}}{2}$$

A. Δ. Ο. (x'x) (1+)

$$m_1 \cdot U_1 = (m_1 + m_2) \cdot U_{Kx} \Rightarrow 8 = 4 \cdot U_K \cdot \frac{\sqrt{2}}{2} \Rightarrow U_K = \frac{4}{\sqrt{2}} = \frac{4 \cdot \sqrt{2}}{2}$$

$$\Rightarrow \boxed{U_K = 2 \cdot \sqrt{2} \text{ m/s}}$$

A. Δ. Ο. (y'y) (1+)

$$m_2 \cdot U_2 = (m_1 + m_2) \cdot U_{Ky} \Rightarrow 2 \cdot U_2 = 4 \cdot U_K \cdot \frac{\sqrt{2}}{2} \Rightarrow 2 \cdot U_2 = 4 \cdot 2 \cdot \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{2}}{2}$$

$$\Rightarrow \boxed{U_2 = 4 \text{ m/s}}$$

Δ2 $\pi = ?$

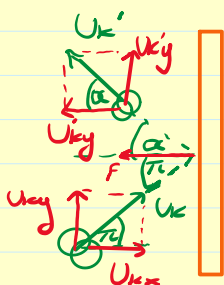
$$K_{ολητηρινι} = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} \cdot 2 \cdot 4^2 + \frac{1}{2} \cdot 2 \cdot 4^2 = 32 \text{ J}$$

$$K_{ολημετωι} = \frac{1}{2} (m_1 + m_2) v_k^2 = \frac{1}{2} \cdot 4 \cdot (2\sqrt{2})^2 = 16 \text{ J}$$

$$Q_{κρ} = K_{ολητηρινι} - K_{ολημετωι} = 16 \text{ J}$$

$$\pi = \frac{Q_{κρ}}{K_{ολητηρινι}} \cdot 100\% = \frac{16}{32} \cdot 100\% \Rightarrow \pi = 50\%$$

Δ3 N. Δ. O. : $\pi = \alpha$



Ελαστικη.

$$K_{τηρινι} = K_{μετωι} \Rightarrow \frac{1}{2} m_1 v_k^2 = \frac{1}{2} m_1 v_k'^2$$

$$\Rightarrow v_k = v_k'$$

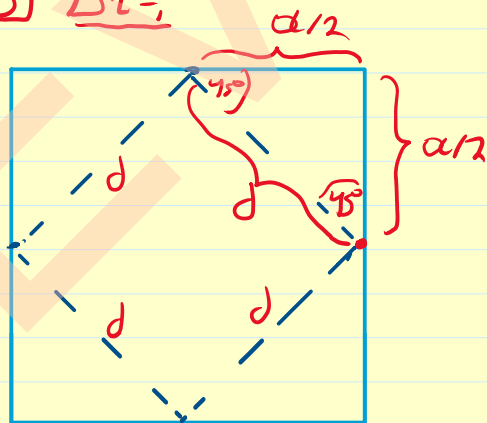
A. Δ. O. (y-y) : $m_1 v_{ky} = m_2 v_{k'y} \Rightarrow v_k \cdot \eta \mu \alpha = v_k' \cdot \eta \mu \alpha$
 $\Rightarrow \pi = \alpha$

Δ4 $F = ?$

$$2\vec{F}_x = \frac{\Delta \vec{p}_x}{\Delta t} \stackrel{(+)}{\Rightarrow} F = \frac{m_2 v_{k'x} - (-m_2 v_{kx})}{\Delta t} = \frac{2 \cdot m_2 \cdot v_k \cdot \alpha \mu \varphi}{\Delta t}$$

$$\Rightarrow F = \frac{2 \cdot 4 \cdot 2\sqrt{2} \cdot \frac{\sqrt{2}}{2}}{0,02} \Rightarrow F = 800 \text{ N}$$

Δ5 $\Delta t = ?$



$$d = \sqrt{\frac{a^2}{4} + \frac{a^2}{4}} = \frac{a\sqrt{2}}{2} = 0,25\sqrt{2} \text{ m}$$

• Διαμειρα ατωστωιων $\Delta x = 4d$

$$v_k = \frac{\Delta x}{\Delta t} \Rightarrow \Delta t = \frac{\Delta x}{v_k} = \frac{4d}{v_k}$$

$$\Rightarrow \Delta t = \frac{\sqrt{2}}{2\sqrt{2}} \Rightarrow \Delta t = 0,5 \text{ s}$$