

ΘΕΜΑ Α

A1) β A2) α A3) γ A4) δ

A5) α) ^ β) ε γ) ε δ) ε ε) ε

ΘΕΜΑ Β

B1 Ψωφί απάντηση η (γ)

Ψωφί s_1 :

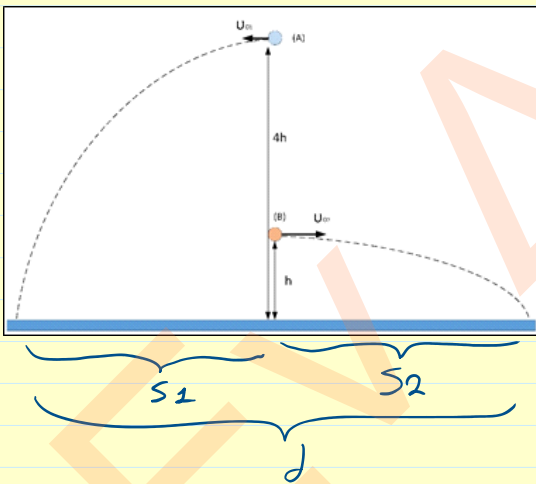
$$t_{\epsilon\sigma 1} = \sqrt{\frac{2h_1}{g}} = \sqrt{\frac{2 \cdot 4h}{g}} = 2 \cdot \sqrt{\frac{2h}{g}}$$

ΒΕΩΝΕΥΕΣ: $s_1 = v_{01} \cdot t_{\epsilon\sigma 1} \Rightarrow s_1 = 2 \cdot v_{01} \cdot \sqrt{\frac{2h}{g}}$

Ψωφί s_2 :

$$t_{\epsilon\sigma 2} = \sqrt{\frac{2 \cdot h_2}{g}} = \sqrt{\frac{2 \cdot h}{g}}$$

ΒΕΩΝΕΥΕΣ: $s_2 = v_{02} \cdot t_{\epsilon\sigma 2} \Rightarrow s_2 = 3 \cdot v_{02} \cdot \sqrt{\frac{2h}{g}}$

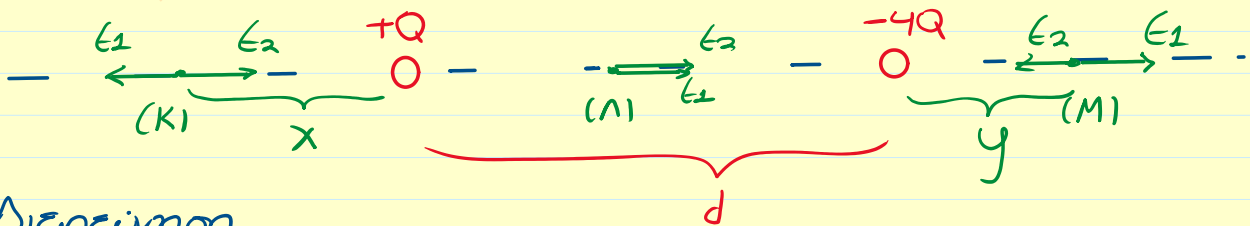


$$d = s_1 + s_2$$

$$\Rightarrow d = 2 \cdot v_{01} \cdot \sqrt{\frac{2h}{g}} + 3 \cdot v_{02} \cdot \sqrt{\frac{2h}{g}}$$

$$\Rightarrow d = 5 \cdot v_{01} \cdot \sqrt{\frac{2h}{g}}$$

B2 Ψωφί απάντηση η (β)



Διερεύνηση

→ Σημείο Λ: $\vec{E}_1 \uparrow \uparrow \vec{E}_2$, ορα $\epsilon_{02\kappa 1} \neq 0$

→ Σημείο Μ:

$$\left. \begin{aligned} E_1 &= k_c \cdot \frac{|Q_1|}{(d+y)^2} \\ E_2 &= k_c \cdot \frac{|Q_2|}{y^2} \end{aligned} \right\} \frac{|Q_1| < |Q_2|}{(d+y)^2 > y^2} \Rightarrow E_1 < E_2, \text{ άρα } \epsilon_{\sigma\kappa\mu} \neq 0$$

→ Σημείο Κ:

$$\epsilon_{\sigma\kappa\mu} = 0 \Rightarrow E_1 = E_2 \Rightarrow \cancel{k_c} \cdot \frac{|Q_1|}{x^2} = \cancel{k_c} \cdot \frac{|Q_2|}{(d+x)^2}$$

$$\Rightarrow \frac{\cancel{Q}}{x^2} = \frac{4\cancel{Q}}{(d+x)^2} \Rightarrow \left(\frac{d+x}{x}\right)^2 = 4 \Rightarrow \frac{d+x}{x} = \pm 2$$

$$\bullet \frac{d+x}{x} = 2 \Rightarrow d+x = 2x \Rightarrow \boxed{x=d}$$

$$\bullet \frac{d+x}{x} = -2 \Rightarrow d+x = -2x \Rightarrow -3x = d \Rightarrow x = -\frac{d}{3} \text{ Απορ.}$$

B3 i) Ίσωση απάτησης η (γ)

$$H = 5 \Rightarrow \frac{1}{2} g t^2 = v_0 t \Rightarrow t \left(\frac{g}{2} t - v_0 \right) = 0$$

$$\rightarrow t = 0$$

ή

$$\rightarrow \frac{g}{2} t - v_0 = 0 \Rightarrow \boxed{t = \frac{2v_0}{g}}$$

ii) Ίσωση απάτησης η (β)

Όταν φτάνει στο έδαφος:

$$H = \frac{1}{2} g t^2 = \frac{1}{2} g \left(\frac{2v_0}{g} \right)^2 = \frac{1}{2} \cdot g \cdot \frac{4v_0^2}{g^2} \Rightarrow H = \frac{2v_0^2}{g}$$

Όταν η ταχύτητα των ελασ $U = 2v_0$:

$$\bullet U^2 = U_x^2 + U_y^2 \Rightarrow (2v_0)^2 = v_0^2 + U_y^2 \Rightarrow 4v_0^2 - v_0^2 = U_y^2 \\ \Rightarrow U_y = \sqrt{3} \cdot v_0$$

$$\bullet U_y = g \cdot t_1 \Rightarrow \sqrt{3} \cdot v_0 = g \cdot t_1 \Rightarrow t_1 = \frac{\sqrt{3} \cdot v_0}{g}$$

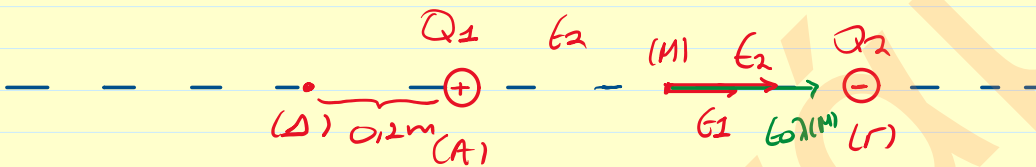
$$y_1 = \frac{1}{2} g t_1^2 = \frac{1}{2} g \left(\frac{\sqrt{3} \cdot U_0}{g} \right)^2 = \frac{1}{2} g \frac{3 \cdot U_0^2}{g^2} \Rightarrow y_1 = \frac{3}{2} \cdot \frac{U_0^2}{g}$$

Άρα, απ' το έδαφος:

$$h_1 = H - y_1 = \frac{2U_0^2}{g} - \frac{3}{2} \cdot \frac{U_0^2}{g} \Rightarrow h_1 = \frac{U_0^2}{2g}$$

ΘΕΜΑ Γ

Γ1) Εορ(μ) = ;



$$E_1 = k_c \cdot \frac{|Q_1|}{(AM)^2} = 9 \cdot 10^9 \cdot \frac{10 \cdot 10^{-6}}{(10^{-2})^2} = \frac{9 \cdot 10^4}{10^{-2}} \Rightarrow E_1 = 9 \cdot 10^6 \text{ N/C}$$

$$E_2 = k_c \cdot \frac{|Q_2|}{(BM)^2} = 9 \cdot 10^9 \cdot \frac{2 \cdot 10 \cdot 10^{-6}}{(10^{-2})^2} = \frac{18 \cdot 10^4}{10^{-2}} \Rightarrow E_2 = 18 \cdot 10^6 \text{ N/C}$$

$$E_{ορ(μ)} = E_2 + E_1 \Rightarrow E_{ορ(μ)} = 27 \cdot 10^6 \text{ N/C}$$

Γ2) V_M = ;

→ Στο σημείο M:

$$V_1 = k_c \cdot \frac{Q_1}{(AM)} = 9 \cdot 10^9 \cdot \frac{10 \cdot 10^{-6}}{10^{-2}} \Rightarrow V_1 = 9 \cdot 10^5 \text{ V}$$

$$V_2 = k_c \cdot \frac{Q_2}{(BM)} = 9 \cdot 10^9 \cdot \frac{-2 \cdot 10 \cdot 10^{-6}}{10^{-2}} \Rightarrow V_2 = -18 \cdot 10^5 \text{ V}$$

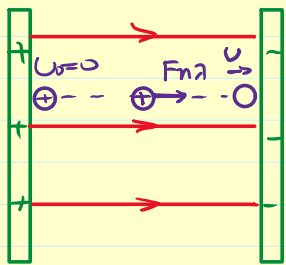
$$V_M = V_1 + V_2 \Rightarrow V_M = -9 \cdot 10^5 \text{ V}$$

Γ3 $W_{F_{\text{ηλ}}}^{M \rightarrow \omega} = ?$

$$W_{F_{\text{ηλ}}}^{M \rightarrow \Delta} = q \cdot (V_M - V_{\infty}) = 2 \cdot 10^{-6} (-9 \cdot 10^3 - 0)$$

$$\Rightarrow W_{F_{\text{ηλ}}}^{M \rightarrow \Delta} = -1,8 \text{ J}$$

Γ4 $\alpha = ?$



$$E = \frac{V}{l} = \frac{40}{8 \cdot 10^{-2}} \Rightarrow E = 500 \text{ N/C}$$

$$F_{\text{ηλ}} = E \cdot |q| = 500 \cdot 2 \cdot 10^{-6} \Rightarrow F_{\text{ηλ}} = 10^{-3} \text{ N}$$

$$\alpha = \frac{F_{\text{ηλ}}}{m} = \frac{10^{-3}}{10^{-3}} \Rightarrow \alpha = 1 \text{ m/s}^2$$

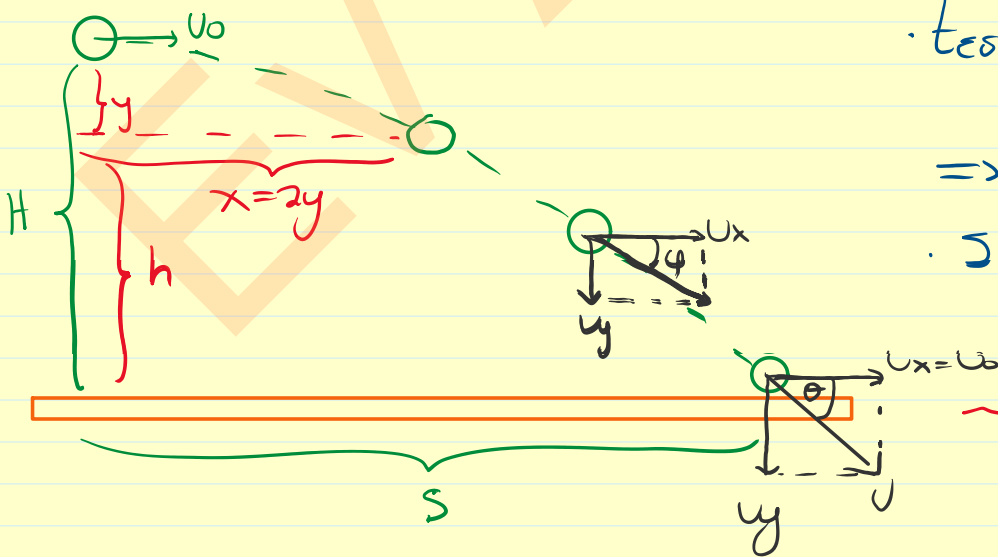
Γ5 $t = ? , v = ?$

$$l = \frac{1}{2} \alpha t^2 \Rightarrow 8 \cdot 10^{-2} = \frac{1}{2} \cdot 1 \cdot t^2 \Rightarrow t = \sqrt{16 \cdot 10^{-2}} \Rightarrow t = 0,4 \text{ s}$$

$$v = \alpha \cdot t \Rightarrow v = 0,4 \text{ m/s}$$

ΘΕΜΑ Δ

Δ1) S = ?



$$t_{\text{εσ}} = \sqrt{\frac{2H}{g}} = \sqrt{\frac{2 \cdot 80}{10}}$$

$$\Rightarrow t_{\text{εσ}} = 4 \text{ s}$$

$$S = v_0 \cdot t_{\text{εσ}} \Rightarrow S = 120 \text{ m}$$

$\rightarrow (v_y = 0)$

$$\Delta 2 \quad U = ?$$

$$\left. \begin{array}{l} U_x = U_0 = 30 \text{ m/s} \\ U_y = g \cdot t_{\text{as}} = 40 \text{ m/s} \end{array} \right\} \Rightarrow U = \sqrt{U_x^2 + U_y^2} \Rightarrow U = 50 \text{ m/s}$$

$$\Delta 3 \quad K = ? \quad , \quad \text{εφ. } \varphi = \frac{1}{3}$$

$$\text{εφ. } \varphi = \frac{1}{3} = \frac{U_y}{U_x} \Rightarrow U_y = \frac{U_x}{3} = \frac{30}{3} \Rightarrow U_y = 10 \text{ m/s}$$

$$K = \frac{1}{2} m \cdot U^2 = \frac{1}{2} m \cdot (\sqrt{U_x^2 + U_y^2})^2 = \frac{1}{2} \cdot 2 \cdot (30^2 + 10^2)$$

$$\Rightarrow K = 1000 \text{ J}$$

$$\Delta 4 \quad x = 6y \quad , \quad \mathcal{U} = ?$$

$$x = 6y \Rightarrow v_0 t = \frac{2}{2} g \cdot t^2 \Rightarrow 10t^2 - 30t = 0$$

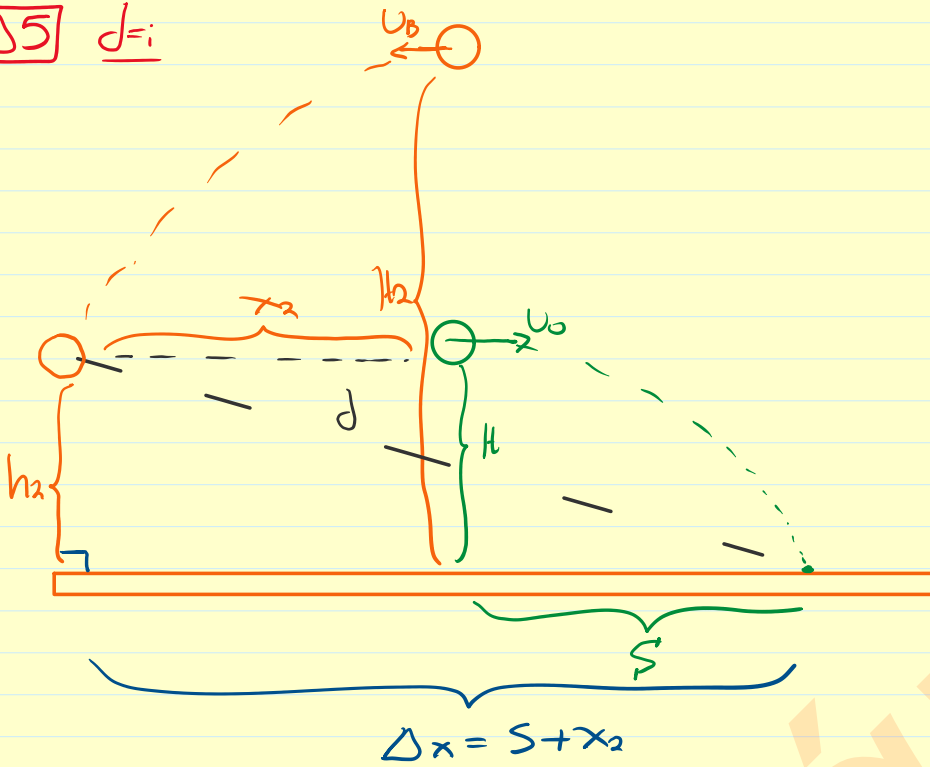
$$\Rightarrow 10t(t-3) = 0 \Rightarrow t = 0 \quad \text{η} \quad t = 3 \text{ s}$$

$$\leadsto y = \frac{1}{2} g \cdot t^2 \Rightarrow y = 45 \text{ m}$$

$$\text{Απ' } \omega \text{ εδωρας: } h = H - y \Rightarrow h = 35 \text{ m}$$

$$\mathcal{U} = m \cdot g \cdot h \Rightarrow \mathcal{U} = 700 \text{ J}$$

$\Delta 5$ $d=i$



Όταν το σωμα Α φτάσει στο έδαφος, το σωμα Β, έχει διανύσει:

$$x_2 = U_0 \cdot t_{\text{εξ}} = 10 \cdot 4 = 40 \text{ m}$$

$$y_2 = \frac{1}{2} \cdot g \cdot t_{\text{εξ}}^2 = \frac{1}{2} \cdot 10 \cdot 4^2 = 80 \text{ m}$$

$$h_2 = H_2 - y_2 = 120 \text{ m}$$

Με βάση το σχήμα:

$$d = \sqrt{\Delta x^2 + h_2^2} = \sqrt{160^2 + 120^2} = \sqrt{25600 + 14400} = \sqrt{40.000}$$

$$\Rightarrow \boxed{d = 200 \text{ m}}$$